## Commutative Algebra (MTH-518/618)

SURPRISE QUIZ (11/09/2017)

Time: 45 minutes Maximum Marks: 10

## Attempt all questions. Use separate page for each answer.

**Problem 1.** Let M be an Artinian A-module and  $\phi : M \to M$  be a module homomorphism. If  $\phi$  is injective then show that  $\phi$  is isomorphism. (4)

**Problem 2.** Let M be an A-module and let I be the annihilator of M in A. Prove that A/I is a Noetherian ring. (3)

**Problem 3.** Find all primary, radical ideal of  $\mathbb{Z}$ . Also compute  $Ass(m\mathbb{Z})$ . (3)